

MATH-7B Sample Test 3

100 points

NAME: \_\_\_\_\_

Show all work neatly. EXACT answers unless specified.

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(1) Given the vectors  $\mathbf{u} = 2\mathbf{i} + 2\mathbf{j}$  and  $\mathbf{v} = -4\mathbf{i} + 3\mathbf{j}$ , find the following:

a)  $\|\mathbf{u}\|$  \_\_\_\_\_

b)  $\mathbf{u} + \mathbf{v}$  \_\_\_\_\_

c)  $\mathbf{u} \cdot \mathbf{v}$  \_\_\_\_\_

d) The angle between  $\mathbf{u}$  and  $\mathbf{v}$  \_\_\_\_\_

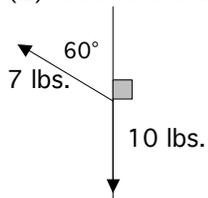
e) The direction angle of  $\mathbf{v}$  (exact) \_\_\_\_\_

f) Find a value for  $b$  such that  $\langle b, 2 \rangle$  is orthogonal to  $\mathbf{v}$  \_\_\_\_\_

g) Find a value for  $c$  such that  $\langle 8, c \rangle$  is parallel to  $\mathbf{v}$  \_\_\_\_\_

h) If  $\mathbf{PQ}$  is a representative of  $\mathbf{v}$  where  $P=(3,-1)$ , find the coordinates of point  $Q$ . \_\_\_\_\_

(2) Two forces act on an object as shown. Find the magnitude and the direction of the resultant.



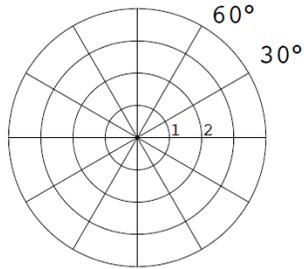
(exact and approx.)

(10 pts)

(3) An airplane is traveling at a constant airspeed of 450 mph in the direction  $N45^\circ W$ . If wind is blowing directly northward at a rate of 50 mph, what is the actual speed and direction of the airplane?

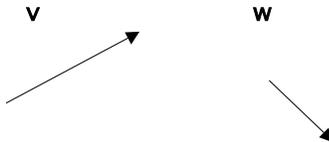
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(4) On the axes below, plot (and label) the polar points  $A(2, 150^\circ)$ ,  $B(3, -\pi/6)$ ,  $C(-2, \pi/2)$  (3pts)



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(5) Given the vectors  $\mathbf{w}$  and  $\mathbf{v}$  below, find  $\mathbf{w} + \mathbf{v}$  and  $-2\mathbf{v}$ .



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(6) Given the point  $(5, 7\pi/4)$  in polar coordinates, find the rectangular representation.

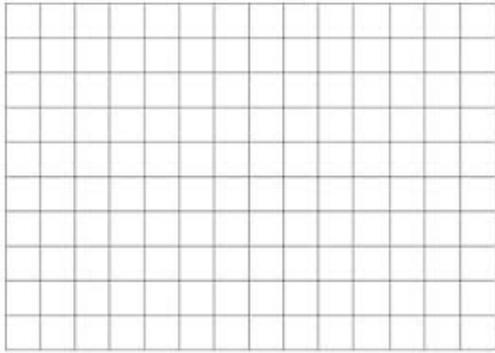
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(7) Given the point  $(-1, \sqrt{3})$  in rectangular coordinates, find two different polar representations; one with  $r > 0$ , the other with  $r < 0$ .

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(8) Convert to rectangular coordinates:  $r \sec\theta = 4$

(9) Graph the polar curve:  $r = 2+2\cos\theta$ .

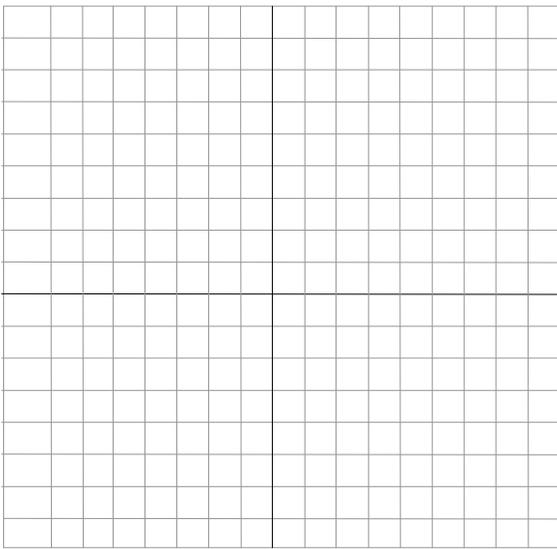


(10) Graph the polar curve:  $r = -4\sin 3\theta$ .



(11) Carefully sketch the graph of  $9x^2 + 4y^2 - 72x + 8y + 112 = 0$ , and find the following desired information. Label at least 2 points on your graph and show scale. (11 points)

VERTICES: \_\_\_\_\_ FOCI: \_\_\_\_\_ COVERTICES: \_\_\_\_\_



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(12) Carefully sketch the graph of  $2x^2 + 8y + 4x - 14 = 0$ , and find the following desired information. Label at least 2 points on your graph and show scale. (11 points)

VERTEX: \_\_\_\_\_ FOCUS: \_\_\_\_\_

